











How can we determine similarity/distance

• if we have a mix of discrete/continuous features:

$$d(\mathbf{x}^{(i)}, \mathbf{x}^{(j)}) = \sum_{f} \begin{cases} \left| x_{f}^{(i)} - x_{f}^{(j)} \right| & \text{if } f \text{ is continuous} \\ 1 - \delta \left(x_{f}^{(i)}, x_{f}^{(i)} \right) & \text{if } f \text{ is discrete} \end{cases}$$

- typically want to apply to continuous features some type of normalization (values range 0 to 1) or standardization (values distributed according to standard normal)
- many other possible distance functions we could use...



• given the training set D, determine the mean and stddev for feature x_i

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$$\mu_{i} = \frac{1}{|D|} \sum_{d=1}^{|D|} x_{i}^{(d)} \qquad \sigma_{i} = \sqrt{\frac{1}{|D|} \sum_{d=1}^{|D|} \left(x_{i}^{(d)} - \mu_{i}\right)^{2}}$$

• standardize each value of feature x_i as follows

$$\hat{x}_i^{(d)} = \frac{x_i^{(d)} - \mu_i}{\sigma_i}$$

- do the same for test instances, using the same μ_i and σ_i derived from the training data













Finding nearest neighbors in a k-d tree	
NearestNeighbor(instance $x^{(q)}$)	
PQ = { }	// minimizing priority queue
best_dist = ∞	// smallest distance seen so far
PQ.push(root, 0)	
while PQ is not empty	
(node, bound) = PQ.pop();	
if (bound ≥ best_dist)	
return best_node.instance	// nearest neighbor found
dist = distance($x^{(q)}$, node. instance)	
if (dist < best_dist)	
best_dist = dist	
best_node = node	
if $(q[node.feature] - node.threshold > 0)$	
PQ.push(node.left, x ^(q) [node.feature] – node.threshold)	
PQ.push(node.right, 0)	
else	
PQ.push(node.left, 0)	
PQ.push(node.right, node. threshold - x ^(q) [node.feature])	
return best_node. instance	







Decally weighted regression prediction/learning task • find the weights w_i for each $x^{(q)}$ by minimizing $E(\mathbf{x}^{(q)}) = \sum_{i=1}^{k} (f(\mathbf{x}^{(i)}) - y^{(i)})^2$ • this is done at prediction time, specifcally for $x^{(q)}$ • can do this using gradient descent (to be covered soon)



Limitations of instance-based learning sensitive to range of feature values sensitive to irrelevant and correlated features, although... there are variants (such as locally weighted regression) that learn weights for different features later we'll talk about *feature selection* methods classification/prediction can be inefficient, although edited methods and *k-d* trees can help alleviate this weakness doesn't provide much insight into problem domain because there is no explicit model