

Diagnostics of ANOVA Model and Multiple Comparison

(Review of lecture examples and R function learning)

1. Steps of Working on ANOVA Model**1.1 Load data into R**

- 1) Create your dataset using notepad(save as .txt) or excel(save as .csv)
- 2) Set the working directory using **setwd()**
- 3) Import data using **read.table()** for .txt file and **read.csv()** for .csv file

1.2 Fit an ANOVA model use **aov(y~x, data=) function**

- 1) y is the response. For example, you want to compare the mean weight of several groups of rats, then the weight is y.
- 2) x is the variable indicating groups

1.3 Checking the model assumptions

- 1) Underlying populations normally distributed: QQ plot of residuals
- 2) Underlying populations have equal variance: residual vs. fitted
- 3) Observations are independent: residuals against index of observation or time order of taking observations and so on.

1.4 Transformation

- 1) Log transformation
When the plot of residuals vs. fitted values show a right-open-mouth horn shape. Use **log()** in R.
- 2) Square transformation
When data are counts. Use **sqrt()** in R.

1.5 Multiple comparisons

- 1) Unplanned comparisons and planned comparisons
- 2) Adjustment of significance level for multiple comparisons – Bonferroni adjustment and Tukey adjustment

2. Example for model assumption checking

2.1 Load data into R

```
il10 <- read.csv("http://www.biostat.wisc.edu/~kbroman/teaching/stat371/il10.csv")
```

The first 15 observations of dataset il10:

Strain	IL10
7	985.425
7	1057.254
7	989.48
7	816.093
7	1410.767
25	1159.141
25	453.573
25	548.546
25	422.12
25	178.64

2.2 Fit an ANOVA model use `aov(y~x, data=)` function

1) Fit model: `aov.il10 <- aov(IL10 ~ Strain, data=il10)`

2) Use `anova()` to get the ANOVA table: `anova(aov.il10)`

Response: IL10

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
Strain	20	33757424	1687871	1.7001	0.04154 *
Residuals	125	124099169	992793		

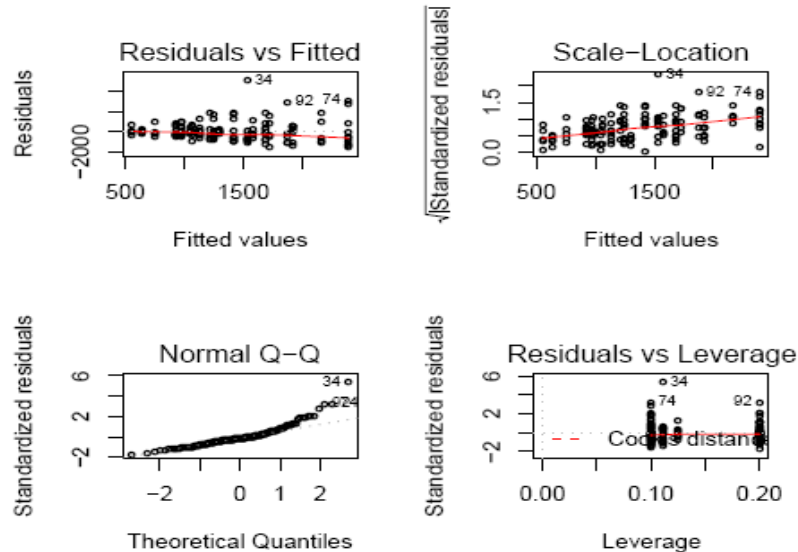
2.3 Checking the model assumptions

1) Underlying populations normally distributed: QQ plot

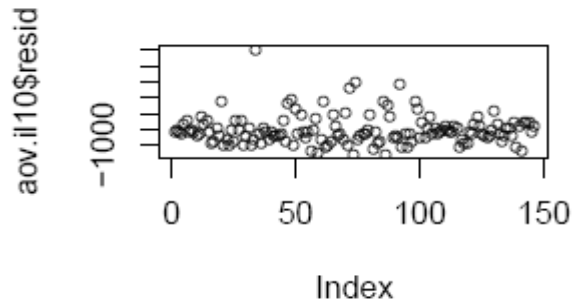
```
par(mfcol=c(2,2)) # specify the layout of plots
```

```
plot(aov.il10, cex=0.7)
```

Four plots, use the 'Normal Q-Q' plot.



- 2) Underlying populations have equal variance: residual plots
Use plot 'Residuals vs Fitted' given in 1).
- 3) Observations are independent within and between groups
Residuals against index of observation: **plot(aov.il10\$resid)**



The residuals are evenly distributed, not correlated, thus independent.

2.4 Transformation

Right-open-mouth horn shape: log transformation

2.5 Refit the ANOVA model using log(IL10) instead of IL10 for response

```
aov.logil10 <- aov(log(IL10) ~ Strain, data=il10)
```

2.6 Check model assumptions for model aov.logil10

3. Example for Multiple Comparisons (Unplanned)

3.1 Use dataset in last Friday's lecture (better use excel to create a dataset)

```
rsp <- c(75,67,70,75,65,71,67,67,76,68,  
        57,58,60,59,62,60,60,57,59,61,  
        58,61,56,58,57,56,61,60,57,58,  
        58,59,58,61,57,56,58,57,57,59,  
        62,66,65,63,64,62,65,65,62,67)  
ttt <- factor(rep(c("C","G","F","G+F","S"),rep(10,5)))  
sugar <- data.frame(rsp, ttt)
```

3.2 Fit ANOVA model

```
aov.out <- aov(rsp ~ ttt, data=sugar)  
anova.out <- anova(aov.out)
```

3.2 Unplanned pair wise comparisons, compare mean response of each pair of groups

1) Bonferroni adjustment

```
source("http://www.biostat.wisc.edu/~kbroman/teaching/stat371/func29.R")
sugar.bonf <- ci.bonf(sugar$rsp, sugar$ttt)
sugar.bonf
```

	est	lower	upper
C - F	11.9	9.09056	14.70944
C - G	10.8	7.99056	13.60944
C - G+F	12.1	9.29056	14.90944
C - S	6.0	3.19056	8.80944
F - G	-1.1	-3.90944	1.70944
F - G+F	0.2	-2.60944	3.00944
F - S	-5.9	-8.70944	-3.09056
G - G+F	1.3	-1.50944	4.10944
G - S	-4.8	-7.60944	-1.99056
G+F - S	-6.1	-8.90944	-3.29056

No significant difference if confidence interval covers 0.

2) Tukey adjustment

```
sugar.tuk <- TukeyHSD(aov.out)
sugar.tuk$ttt
```

	diff	lwr	upr	p adj
F-C	-11.9	-14.868072	-8.931928	3.370637e-13
G-C	-10.8	-13.768072	-7.831928	2.079004e-12
G+F-C	-12.1	-15.068072	-9.131928	3.010925e-13
S-C	-6.0	-8.968072	-3.031928	7.223105e-06
G-F	1.1	-1.868072	4.068072	8.291029e-01
G+F-F	-0.2	-3.168072	2.768072	9.996878e-01
S-F	5.9	2.931928	8.868072	9.983469e-06
G+F-G	-1.3	-4.268072	1.668072	7.256157e-01
S-G	4.8	1.831928	7.768072	3.242398e-04
S-G+F	6.1	3.131928	9.068072	5.222269e-06